

# NEW MATERIALS OF $B_2O_3$ – $Bi_2O_3$ – $Me_2O_3$ (Me = Yb, Lu) SYSTEMS

M.M. Asadov and N.A. Akhmedova

*Institute of Chemical Problems, National Academy of Sciences of Azerbaijan,  
29, G. Javid ave., AZ 1143, Baku, Azerbaijan*

*E-mail: mirasadov@gmail.com*

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## Abstract

It is shown that the  $Yb_2O_3$ – $Bi_2O_3$ – $B_2O_3$  system gives a new  $Yb_3Bi_2B_5O_{15}$  compound of a hexagonal crystallographic system. Based on the data on the nature of specimens and by means of X-ray study of obtained samples, we determined the boundaries of glass-formation regions in the  $Yb_2O_3$ – $Bi_2O_3$ – $B_2O_3$  system. Homogeneous glasses were obtained in the following cuts:  $Bi_2O_3 \cdot B_2O_3$  –  $Lu_2O_3$ – $B_2O_3$  up to 15 mol %  $Lu_2O_3$ ;  $Lu_2O_3 \cdot B_2O_3$ – $Bi_2O_3$  up to 10 mol %  $Lu_2O_3$ ;  $Bi_2O_3 \cdot B_2O_3$  –  $Lu_2O_3 \cdot Bi_2O_3$  up to 15 mol %  $Lu_2O_3$ . Eutectic coordinates of  $LnBO_3$ – $B_2O_3$  (Ln = Ce, Pr, Pm, Sm, Tb, Er) systems were calculated at first.

## 1. Introduction

Multicomponent oxide materials play an important role for finding and creating new functional inorganic materials. Materials based on complex oxides of rare earth metals have a variety of physical and physicochemical properties. These materials can be used as optical materials, oxygen sensors, ionic conductors, catalysts, etc. A wide range of transparency of borates (200–3500 nm) allows you to use these materials in the UV spectral region. In these materials, acentric structural units based on polyborate anions are present. This enhances their nonlinear optical properties. In addition  $Bi_2O_3$ -based materials have high values of the refractive index, a broad region of transparency in the visible and infrared ranges [1–13].

Phase relationships of the boundary sections of  $Yb_2O_3$ – $Bi_2O_3$ – $B_2O_3$  have been previously investigated. Phase equilibria in the  $Bi_2O_3$ – $B_2O_3$  system were studied in [2, 3, 9]. In the  $Bi_2O_3$ – $B_2O_3$  system, in a stable equilibrium, five compounds are found:  $Bi_{24}B_2O_{39}$  (melts incongruently at 905 K),  $Bi_4B_2O_9$ ,  $Bi_3B_5O_{12}$ ,  $BiB_3O_6$  (melt congruently at 948, 995, 981, and 988 K) and  $Bi_{12}B_8O_{15}$ . Connection  $Bi_{12}B_8O_{15}$  experiences a polymorphic transformation at 969 K. Overheated melt during cooling leads to crystallization of metastable phases  $BiBO_3$  and  $Bi_5B_3O_{12}$ .

The  $Yb_2O_3$ – $B_2O_3$  system is characterized by the formation of compounds  $YbBO_3$  and  $Yb_3BO_6$ . The first melts congruently at 1863 K, and the second melts incongruently [10].

Two intermediate compounds  $YbBiO_3$  [12] and  $Yb_7Bi_{17}O_{36}$  ( $x = 0.292$ ) [13] are formed in the  $Yb_2O_3$ – $Bi_2O_3$  system. Binary system components are used, inter alia, to change the properties of ceramics. The process of doping of ceramics  $BaTiO_3$  with components  $Bi_2O_3$  and  $Yb_2O_3$  leads to an increase in the Curie temperature [14].

In this work, we studied the properties in the  $Yb_2O_3$ – $Bi_2O_3$ – $B_2O_3$ ,  $Lu_2O_3$ – $B_2O_3$ – $Bi_2O_3$  and  $LnBO_3$ – $B_2O_3$  systems.

## 2. Experimental

Studies of phase equilibria in the  $\text{Me}_2\text{O}_3\text{--Bi}_2\text{O}_3\text{--B}_2\text{O}_3$  system were carried out using XRD (DRON-2 diffractometer, Cu  $K_{\alpha}$ -radiation, Ni-filter) and DTA (MOM derivatograph) by known methods.  $\text{Me}_2\text{O}_3$  (Me – Yb, Lu) (high purity),  $\text{Bi}_2\text{O}_3$  (high purity) and  $\text{HBO}_3$  (high purity) were used as initial components. The interaction of components was studied on various sections. Synthesis of the samples was carried out in platinum crucibles in a muffle furnace. The duration of synthesis was 15 days.

## 3. Results and discussion

The direction of probable reactions between components of the  $\text{Yb}_2\text{O}_3\text{--Bi}_2\text{O}_3\text{--B}_2\text{O}_3$  system was evaluated by thermodynamic method. Values of Gibbs energy  $\Delta_f G_T^0$  of ternary systems were calculated for the solid state. Thermodynamic data of binary oxides were taken from references [15, 16]. Gibbs energy and enthalpy of formation of ternary compounds were calculated from the data for binary compounds using the equations [17]

$$\Delta V_{T,(1-x)A-xB}^0 = (1-x)\Delta V_{T,A}^0 + x\Delta V_{T,B}^0 + 2x\Delta V_{T,m}^0 \quad (x \leq 0.5) \quad (1)$$

$$\Delta V_{T,(1-x)A-xB}^0 = (1-x)\Delta V_{T,A}^0 + x\Delta V_{T,B}^0 + 2(1-x)\Delta V_{T,m}^0 \quad (x \geq 0.5) \quad (2)$$

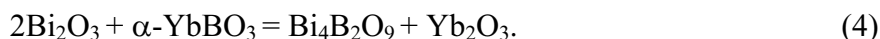
$$\Delta V_{T,(1-x)A-xB}^0 = (1-x)\Delta V_{T,A}^0 + x\Delta V_{T,B}^0 + \Delta V_{T,m}^0 \frac{x(1-x)}{0.25} \quad (3)$$

where  $\Delta V_{T,m}^0$  are values of Gibbs energy  $\Delta_f G_T^0$  and the enthalpy of formation  $\Delta_f H_T^0$  of compounds of oxides with the composition  $x = 0.5$ . Values of  $\Delta_f G_{298}^0$  and  $\Delta_f H_{298}^0$  for the ternary  $\text{Yb}_2\text{O}_3\text{--Bi}_2\text{O}_3\text{--B}_2\text{O}_3$  calculated from equations (1)–(3) are given in Table. 1.

Table 1. The calculated values of Gibbs energy and enthalpy of formation of ternary oxide compounds of the  $\text{Yb}_2\text{O}_3\text{--Bi}_2\text{O}_3\text{--B}_2\text{O}_3$  system.

Compound	$T_f$ (K)	$-\Delta_f H_{298}^0$ (kJ/mol)	$-\Delta_f G_{298}^0$ (kJ/mol)
$\text{Bi}_4\text{B}_2\text{O}_9$	948	1431	1309
$\text{BiBO}_3$	958	1832	1692
$\text{Bi}_3\text{B}_5\text{O}_{12}$	995	1682	1562
$\text{BiB}_3\text{O}_6$	981	1543	1443
$\text{YbBO}_3$	1863	3067	2921
$\text{Yb}_3\text{BO}_6$		2442	2325

The direction of probable reactions was estimated from tabular data. For example, for the reaction



The value of  $\Delta_f G_{298}^0$  in the forward direction is negative:  $-582$  kJ / mol. Evaluation indicates that the change in a temperature range of 298–600 K have a weak effect on the value of  $\Delta_f G_T^0$ . To move from  $\Delta_f G_{298}^0$  to  $\Delta_f G_T^0$ , we used the Kirchhoff equation and value of the specific heat of the components [15]. These thermodynamic evaluations of the probability of a reaction between the corresponding components in the system  $\text{Yb}_2\text{O}_3\text{--Bi}_2\text{O}_3\text{--B}_2\text{O}_3$  are confirmed with the data of physicochemical analysis.

The properties of promising compounds  $\text{BiBO}_3$  are given in [18-24]. The melting point of  $\text{BiBO}_3$  compound is  $955 \pm 5$  K.  $\text{YbBO}_3$  has a polymorphic transformation at 850 and 1314 K according to [9]. The melting temperature of  $\text{YbBO}_3$  is 1863 K.

In order to obtain reliable data, the synthesized phases  $\text{BiBO}_3$  and  $\text{YbBO}_3$  were annealed at 600–625 K for 7 days. The alloys were prepared of these components for physical and chemical analyses.

The phase diagram of the  $\text{BiBO}_3$ – $\text{YbBO}_3$  system constructed by us is shown in Fig. 1.

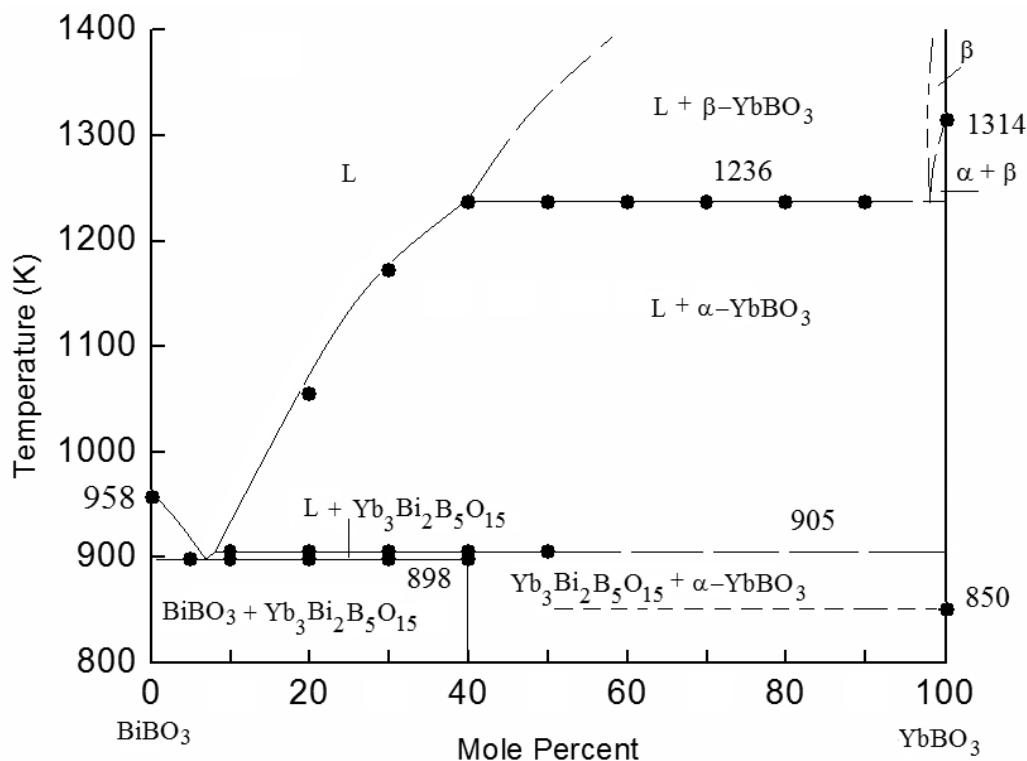


Fig. 1. Phase diagram of the  $\text{BiBO}_3$ – $\text{YbBO}_3$  system.

The figure shows that, in the  $\text{Yb}_2\text{O}_3$ – $\text{Bi}_2\text{O}_3$ – $\text{B}_2\text{O}_3$  system, intermediate phase  $\text{Yb}_3\text{Bi}_2\text{B}_5\text{O}_{15}$  is formed. This compound melts incongruently at 908 K. According to XRD patterns, the samples whose compositions correspond to  $\text{Yb}_3\text{Bi}_2\text{B}_5\text{O}_{15}$  have a hexagonal system and the following cell parameters:  $a = 4.913$  (1),  $c = 16.214$  (1) Å.

The isothermal section of  $\text{Yb}_2\text{O}_3$ – $\text{Bi}_2\text{O}_3$ – $\text{B}_2\text{O}_3$  system at 298 K was constructed as shown in Fig. 2. For this, the data on the boundary systems and data on the phase composition of synthesized samples were used. Isothermal section of the system at 298 K may be represented by 13 triangles of coexisting phases:  $\alpha$ - $\text{Bi}_{12}\text{B}_8\text{O}_{15}$ – $\text{B}_2\text{O}_3$ – $\alpha$ - $\text{YbBO}_3$ ,  $\alpha$ - $\text{Bi}_{12}\text{B}_8\text{O}_{15}$ – $\text{BiB}_3\text{O}_6$ – $\text{YbBO}_3$ ,  $\text{Bi}_3\text{B}_5\text{O}_{12}$ – $\text{BiB}_3\text{O}_6$ – $\alpha$ - $\text{YbBO}_3$ ,  $\text{Bi}_3\text{B}_5\text{O}_{12}$ – $\text{Yb}_3\text{Bi}_2\text{B}_5\text{O}_{15}$ – $\alpha$ - $\text{YbBO}_3$ ,  $\text{Bi}_3\text{B}_5\text{O}_{12}$ – $\text{Yb}_3\text{Bi}_2\text{B}_5\text{O}_{15}$ – $\text{BiBO}_3$ ,  $\text{Bi}_4\text{B}_2\text{O}_9$ – $\text{Yb}_3\text{Bi}_2\text{B}_5\text{O}_{15}$ – $\text{BiBO}_3$ ,  $\text{Bi}_4\text{B}_2\text{O}_9$ – $\text{Yb}_3\text{Bi}_2\text{B}_5\text{O}_{15}$ – $\alpha$ - $\text{YbBO}_3$ ,  $\text{Bi}_4\text{B}_2\text{O}_9$ – $\text{Yb}_3\text{BO}_6$ – $\alpha$ - $\text{YbBO}_3$ ,  $\text{Bi}_4\text{B}_2\text{O}_9$ – $\text{Yb}_3\text{BO}_6$ – $\text{Yb}_2\text{O}_3$ ,  $\text{Bi}_4\text{B}_2\text{O}_9$ – $\alpha$ - $\text{YbBiO}_3$ – $\text{Yb}_2\text{O}_3$ ,  $\text{Bi}_4\text{B}_2\text{O}_9$ – $\alpha$ - $\text{YbBiO}_3$ – $\text{Yb}_7\text{Bi}_{17}\text{O}_{36}$ ,  $\text{Bi}_4\text{B}_2\text{O}_9$ – $\text{Bi}_{24}\text{B}_{20}\text{O}_{39}$ – $\text{Yb}_7\text{Bi}_{17}\text{O}_{36}$ , and  $\text{Bi}_2\text{O}_3$ – $\text{Bi}_{24}\text{B}_{20}\text{O}_{39}$ – $\text{Yb}_7\text{Bi}_{17}\text{O}_{36}$ .

Experimental data on the phase composition of synthesized samples allowed constructing the liquids surface projection of the  $\text{BiBO}_3$ – $\text{B}_2\text{O}_3$ – $\text{YbBO}_3$  system. The temperatures of invariant reactions in this system are given in Table 2.

On the basis of these data about the character of specimens and by means of roentgen-study of obtained samples, we determined the boundaries of glass-formation regions in  $\text{Yb}_2\text{O}_3$ – $\text{Bi}_2\text{O}_3$ – $\text{B}_2\text{O}_3$  system. In the  $\text{Yb}_2\text{O}_3$ – $\text{Bi}_2\text{O}_3$ – $\text{B}_2\text{O}_3$  system, the glass-formation region is tapered in the  $\text{Bi}_2\text{O}_3$ · $\text{B}_2\text{O}_3$ – $\text{Yb}_2\text{O}_3$ · $\text{B}_2\text{O}_3$  cut, but in  $2\text{Bi}_2\text{O}_3$ · $\text{B}_2\text{O}_3$ – $\text{Yb}_2\text{O}_3$ · $\text{B}_2\text{O}_3$  cut at composi-

tions from 10 mol % Bi<sub>2</sub>O<sub>3</sub> to 40 mol % Bi<sub>2</sub>O<sub>3</sub> the glasses with decreased thermal characteristics were revealed (T<sub>melt</sub> = 653 K; T<sub>cr</sub> = 713 K).

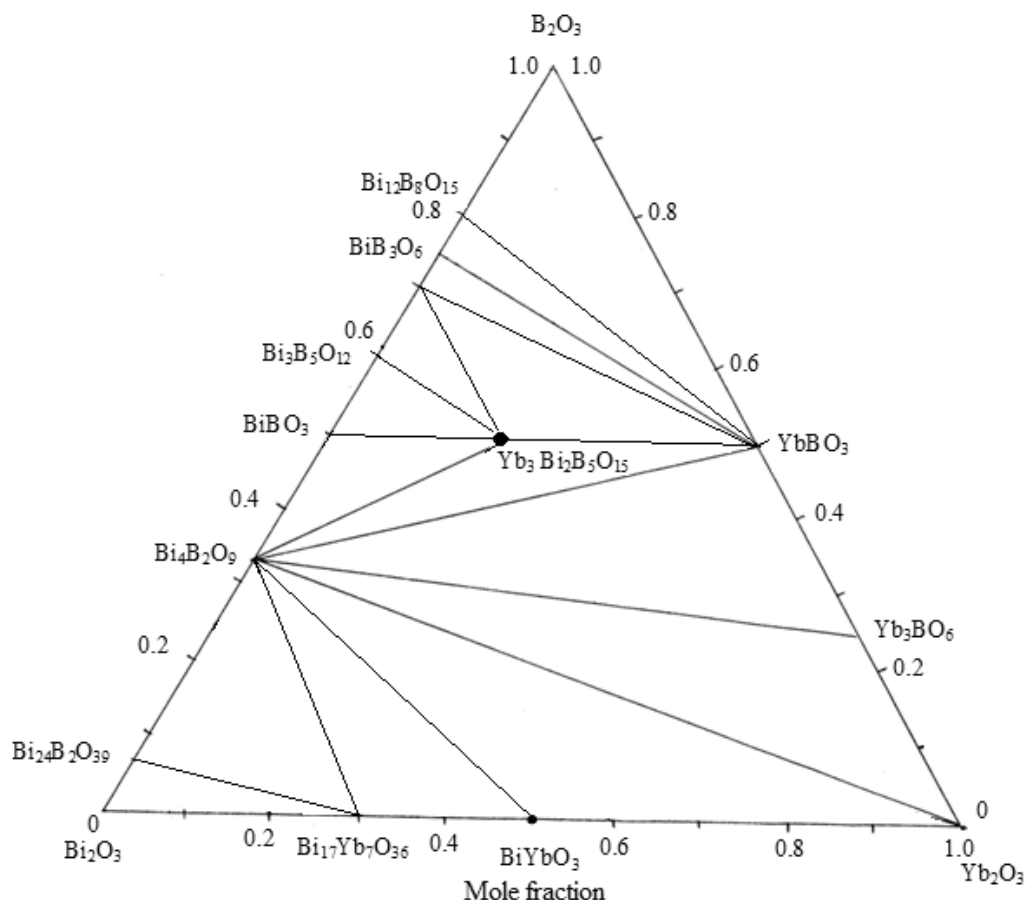


Fig. 2. Isothermal section of the Yb<sub>2</sub>O<sub>3</sub>–Bi<sub>2</sub>O<sub>3</sub>–B<sub>2</sub>O<sub>3</sub> system at 298 K.

Table 2. The temperature of invariant reactions in the BiBO<sub>3</sub>–B<sub>2</sub>O<sub>3</sub>–YbBO<sub>3</sub> system.

Reaction	Reaction type	T, K
$L \leftrightarrow BiYbO_3 + Bi_3B_5O_{12} + Yb_3Bi_2B_5O_{15}$	Eutectic (E <sub>1</sub> )	948
$L \leftrightarrow Bi_3B_5O_{12} + \beta\text{-}YbBO_3 + BiB_3O_6$	Eutectic (E <sub>2</sub> )	973
$L + \beta\text{-}YbBO_3 \leftrightarrow Yb_3Bi_2B_5O_{15} + Bi_3B_5O_{12}$	Peritectic (P <sub>1</sub> )	1088
$L + \beta\text{-}YbBO_3 \leftrightarrow BiB_3O_6 + \beta\text{-}Bi_{12}B_8O_{15}$	Peritectic (P <sub>2</sub> )	1000

The synthesis of Bi<sub>2</sub>O<sub>3</sub>·B<sub>2</sub>O<sub>3</sub> – Lu<sub>2</sub>O<sub>3</sub>·B<sub>2</sub>O<sub>3</sub>, Lu<sub>2</sub>O<sub>3</sub>·B<sub>2</sub>O<sub>3</sub> – Bi<sub>2</sub>O<sub>3</sub>, Lu<sub>2</sub>O<sub>3</sub>·B<sub>2</sub>O<sub>3</sub> – Lu<sub>2</sub>O<sub>3</sub>·Bi<sub>2</sub>O<sub>3</sub>, Bi<sub>2</sub>O<sub>3</sub>·B<sub>2</sub>O<sub>3</sub> – Lu<sub>2</sub>O<sub>3</sub>·Bi<sub>2</sub>O<sub>3</sub> systems was carried out by the solid-state-phase method. The color of specimens was varied from violent yellow to brown. In the Lu<sub>2</sub>O<sub>3</sub> – B<sub>2</sub>O<sub>3</sub> – Bi<sub>2</sub>O<sub>3</sub> system, three regions were revealed: homogenous glasses, crystal compounds and unmixed phases. The boundaries of regions of glass-formation were determined by visually and from X-ray study of obtained specimens. Homogeneous glasses were obtained in the following cuts: Bi<sub>2</sub>O<sub>3</sub>·B<sub>2</sub>O<sub>3</sub>–Lu<sub>2</sub>O<sub>3</sub>·B<sub>2</sub>O<sub>3</sub> up to 15 mol % Lu<sub>2</sub>O<sub>3</sub>; Lu<sub>2</sub>O<sub>3</sub>·B<sub>2</sub>O<sub>3</sub>–Bi<sub>2</sub>O<sub>3</sub> up to 10 mol % Lu<sub>2</sub>O<sub>3</sub>; and Bi<sub>2</sub>O<sub>3</sub>·B<sub>2</sub>O<sub>3</sub> – Lu<sub>2</sub>O<sub>3</sub>·Bi<sub>2</sub>O<sub>3</sub> up to 15 mol % Lu<sub>2</sub>O<sub>3</sub>.

In systems Ln<sub>2</sub>O<sub>3</sub>–Bi<sub>2</sub>O<sub>3</sub>–B<sub>2</sub>O<sub>3</sub> based on “light” lanthanide (Ln = La–Tb) three compounds are crystallized: metaborate LnB<sub>3</sub>O<sub>6</sub>, orthoborate LnBO<sub>3</sub>, and oxoborate

$\text{Ln}_3\text{BO}_6$  [11-13]. In systems  $\text{Ln}_2\text{O}_3\text{--Bi}_2\text{O}_3\text{--B}_2\text{O}_3$  based on “heavy” lanthanides ( $\text{Ln} = \text{Dy--Lu}$ ) only ortho- and oxoborates are crystallized.

Orthoborates are crystallized in different structural types of  $\text{CaCO}_3$  depending on the ionic radii. The types of aragonite ( $\text{La--Nd}$ ), vaterite ( $\text{Sm--Yb, Y}$ ), and calcite ( $\text{Lu}$  and  $\text{Sc}$ ) are stable. Boron atoms are located in isolated  $\text{BO}_3$ -triangles. The location of the structural units of  $\text{BO}_3$ -on  $\text{Ln}$  atom is different for different structural types. High refractive index (1.729–1.755), relatively low boiling temperatures of lanthanum borate glasses as compared with silicate glasses, and transparency in the a of 350–1700 nm make these glasses a promising material for photonics [11].

Correlation equations for calculation of eutectic coordinates in  $\text{LnBO}_3\text{--B}_2\text{O}_3$  ( $\text{Ln} = \text{La, Ce, Pr, Nd, Pm, Sm, Eu, Gd, Tb, Dy, Ho, Er, Tm, Yb, Lu}$ ) systems were proposed. Eutectic coordinates of  $\text{LnBO}_3\text{--B}_2\text{O}_3$  ( $\text{Ln} = \text{Ce, Pr, Pm, Sm, Tb, Er}$ ) systems were calculated at first (Table 3).

Table 3. Calculated coordinates of eutectic in systems  $\text{LnBO}_3\text{--B}_2\text{O}_3$ .

System	$C_e$ , mol % $\text{B}_2\text{O}_3$	$T_e$ , °C	$T_{\text{fus}}$ , °C ( $\text{LnBO}_3$ )	System	$C_e$ , mol % $\text{B}_2\text{O}_3$	$T_e$ , °C	$T_{\text{fus}}$ , °C ( $\text{LnBO}_3$ )
$\text{LaBO}_3\text{--B}_2\text{O}_3$	22	1136	1660	$\text{GdBO}_3\text{--B}_2\text{O}_3$	27	1232	1590
$\text{CeBO}_3\text{--B}_2\text{O}_3$	22	1140	1650	$\text{TbBO}_3\text{--B}_2\text{O}_3$	28	1280	1525
$\text{PrBO}_3\text{--B}_2\text{O}_3$	23	1144	1630	$\text{DyBO}_3\text{--B}_2\text{O}_3$	29	1328	1585
$\text{NdBO}_3\text{--B}_2\text{O}_3$	24	1148	1610	$\text{HoBO}_3\text{--B}_2\text{O}_3$	30	1368	1605
$\text{PmBO}_3\text{--B}_2\text{O}_3$	25	1150	1590	$\text{ErBO}_3\text{--B}_2\text{O}_3$	30	1396	1630
$\text{SmBO}_3\text{--B}_2\text{O}_3$	27	1157	1570	$\text{TmBO}_3\text{--B}_2\text{O}_3$	31	1424	1650
$\text{EuBO}_3\text{--B}_2\text{O}_3$	27	1172	1540	$\text{YbBO}_3\text{--B}_2\text{O}_3$	31	1446	1590
				$\text{LuBO}_3\text{--B}_2\text{O}_3$	32	1473	1650

#### 4. Conclusions

Thus, the isothermal section of phase diagram of  $\text{Yb}_2\text{O}_3\text{--Bi}_2\text{O}_3\text{--B}_2\text{O}_3$  at 298 K, as well as the projection of the liquid surface of  $\text{BiBO}_3\text{--B}_2\text{O}_3\text{--YbBO}_3$ , was firstly constructed. The phase diagram of the polythermal section of  $\text{BiBO}_3\text{--YbBO}_3$  is given. The formation of  $\text{Yb}_3\text{Bi}_2\text{B}_5\text{O}_{15}$  compounds with a hexagonal system and the following cell parameters:  $a = 4.913$ ,  $c = 16.214 \text{ \AA}$  was confirmed. The obtained data can be useful for the preparation of materials with specific composition, structure and properties. On the basis of these data about the character of specimens and by means of X-ray study of obtained samples, we determined the boundaries of glass-formation regions in the  $\text{Yb}_2\text{O}_3\text{--Bi}_2\text{O}_3\text{--B}_2\text{O}_3$  system. In the  $\text{Yb}_2\text{O}_3\text{--Bi}_2\text{O}_3\text{--B}_2\text{O}_3$  system, the glass-formation region is tapered in the  $\text{Bi}_2\text{O}_3\text{·B}_2\text{O}_3\text{--Yb}_2\text{O}_3\text{·B}_2\text{O}_3$  cut, but in  $2 \text{ Bi}_2\text{O}_3\text{·B}_2\text{O}_3\text{--Yb}_2\text{O}_3\text{·B}_2\text{O}_3$  cut for compositions of 10 mol %  $\text{Bi}_2\text{O}_3$  to 40 mol %  $\text{Bi}_2\text{O}_3$ , the glasses with decreased thermal characteristics were revealed ( $T_{\text{melt}} = 653 \text{ K}$ ;  $T_{\text{cr}} = 713 \text{ K}$ ). Correlation equations for calculation of eutectic coordinates in  $\text{LnBO}_3\text{--B}_2\text{O}_3$  ( $\text{Ln} = \text{La, Ce, Pr, Nd, Pm, Sm, Eu, Gd, Tb, Dy, Ho, Er, Tm, Yb, Lu}$ ) systems were proposed. Eutectic coordinates of  $\text{LnBO}_3\text{--B}_2\text{O}_3$  ( $\text{Ln} = \text{Ce, Pr, Pm, Sm, Tb, Er}$ ) systems were calculated at first.

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